

# Spin Hall effect for polaritons in a TMDC monolayer embedded in a microcavity

Oleg L. Berman<sup>1</sup>, Roman Ya. Kezerashvili<sup>1</sup>,  
and Yurii E. Lozovik<sup>2</sup>



*<sup>1</sup>New York City College of Technology,  
The City University of New York*

*<sup>2</sup>Institute of Spectroscopy, Russian Academy of Sciences*

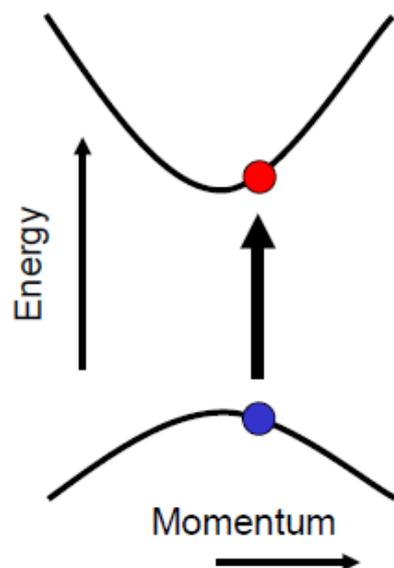
The work was supported by US Department of Defense under  
Grant No. W911NF1810433  
and PSC CUNY  
under Grant No. 60599-00 48.

# OUTLINE

- **EXCITONS AND MICROCAVITY POLARITONS**
- **SPIN HALL EFFECT**
- **EXCITONS IN TMDCs MONOLAYERS**
- **SPIN HALL EFFECT FOR POLARITONS IN  
A TMDC MONOLAYER EMBEDDED IN  
A MICROCAVITY**
- **CONCLUSIONS**

# Making light atoms inside a solid

Excite electron-hole pair across a semiconductor band gap

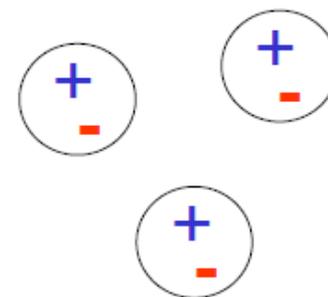


Bound by the screened Coulomb interaction to make an exciton

$$Ry^* = \frac{m^*/m}{\epsilon^2} \times \text{Rydberg}$$

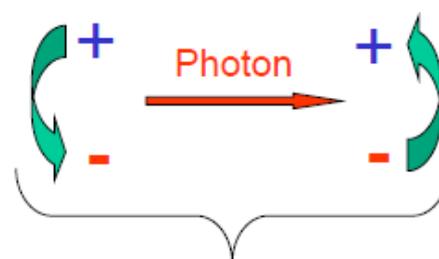
$$a_0^* = \frac{\epsilon}{m^*/m} \times a_{Bohr}$$

Polariton Effective Mass  $m^* \sim 10^{-4} m_e$   
 $T_{BEC} \sim 1/m^*$



**Excitons** are the solid state analogue of positronium  
In GaAs

Binding energy  $\sim 5$  meV  
Bohr Radius  $\sim 7$  nm

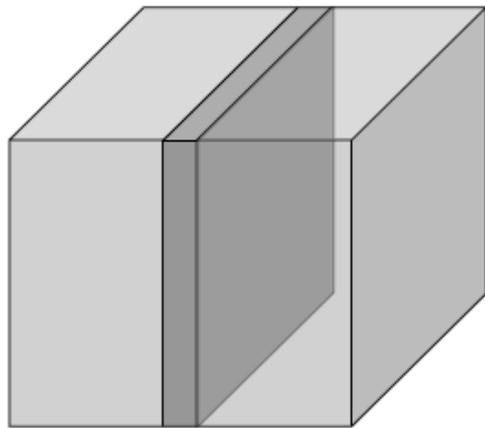


Combined coherent excitation is called a **polariton**

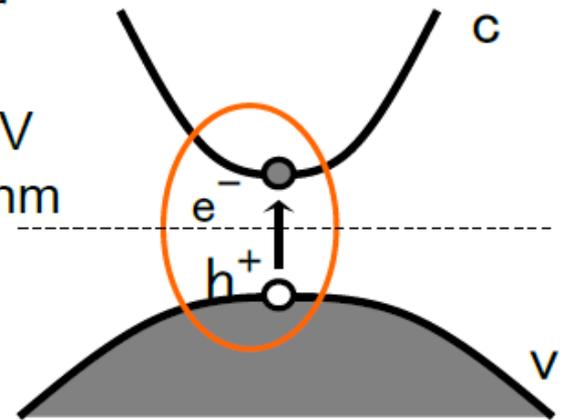
# Quantum Well Excitons

Weakly bound  
electron-hole pair  
**EXCITON**

Rydberg – few meV  
Bohr Radius – few nm



QW



energy

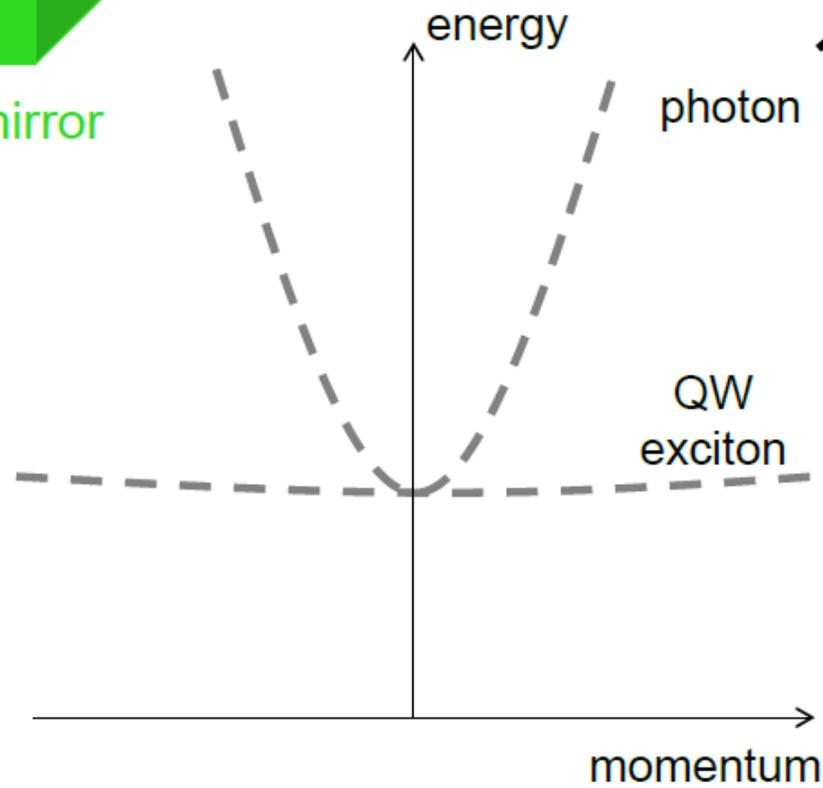
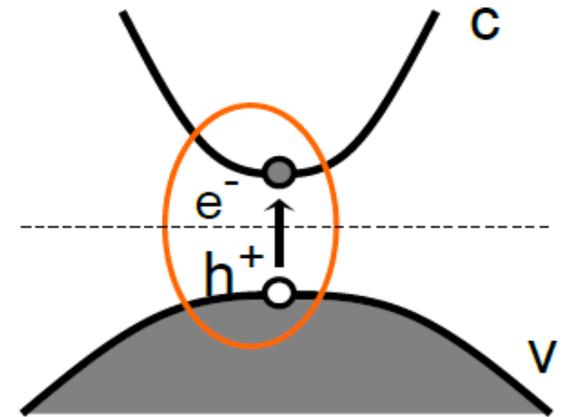
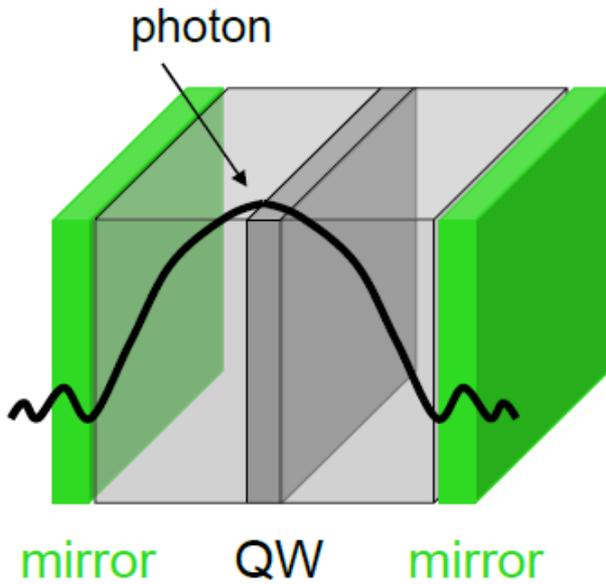
particle-hole  
continuum

Excitation spectrum

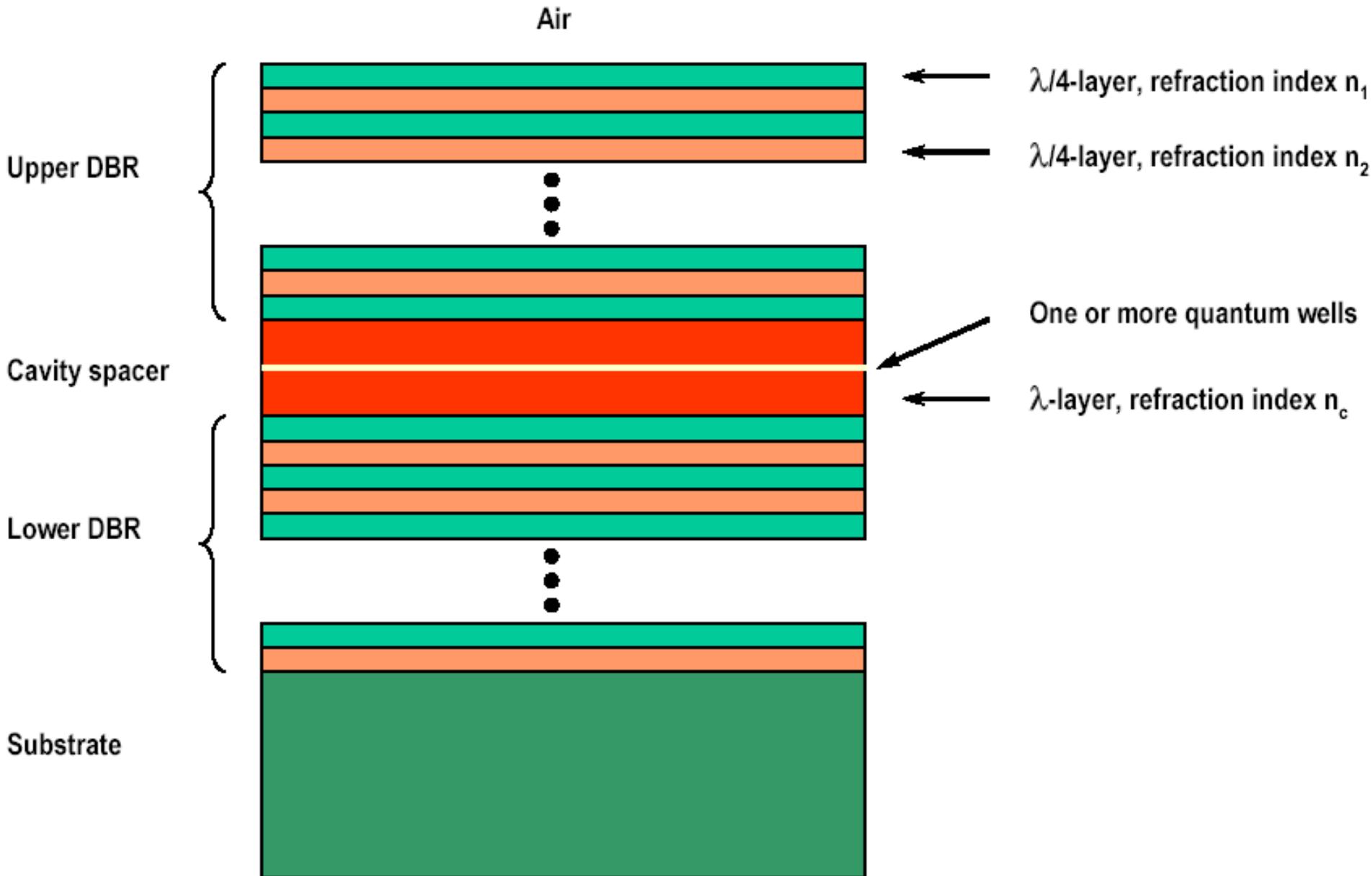
QW  
exciton

in-plane center of mass momentum

# Excitons + Cavity Photons

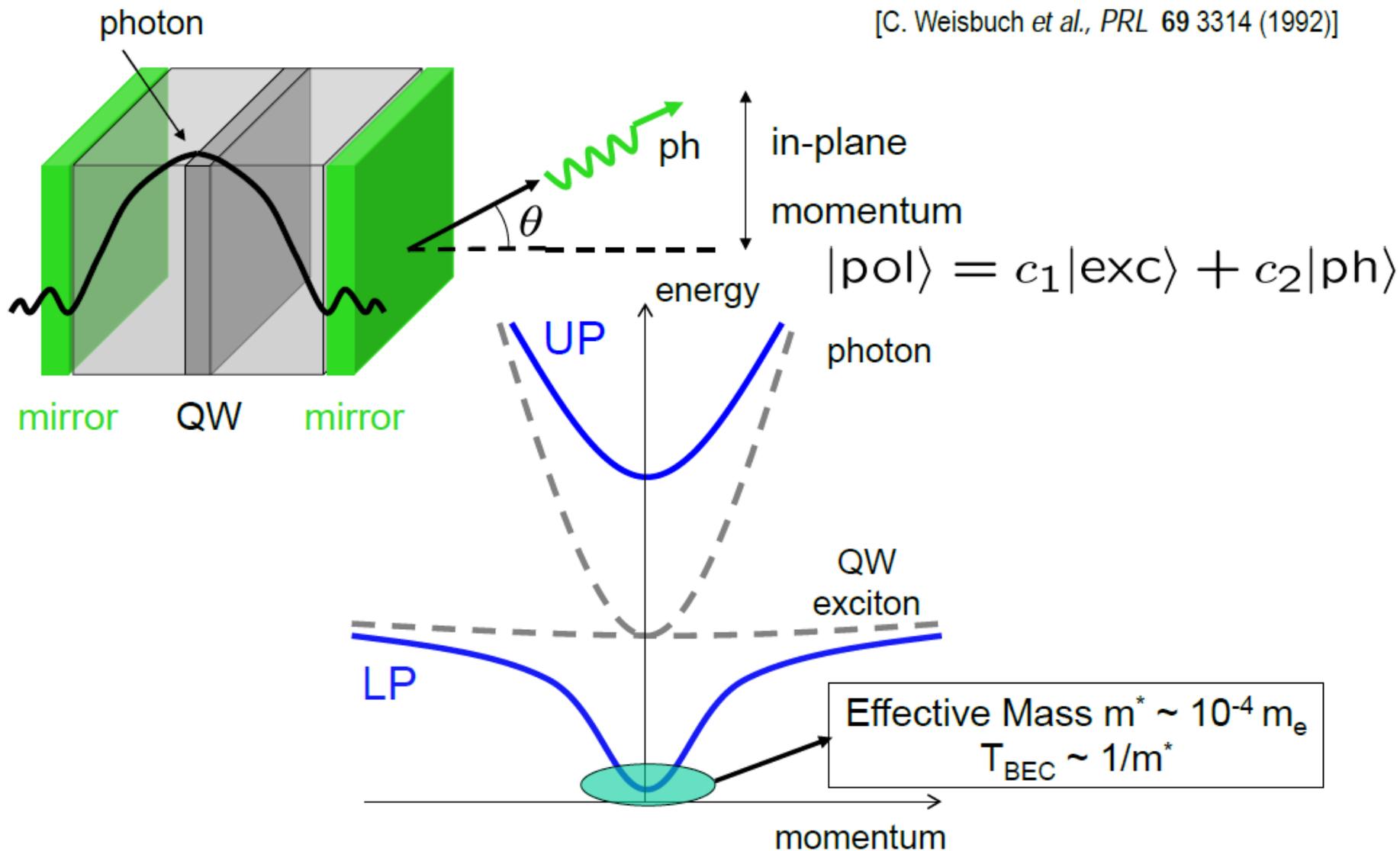


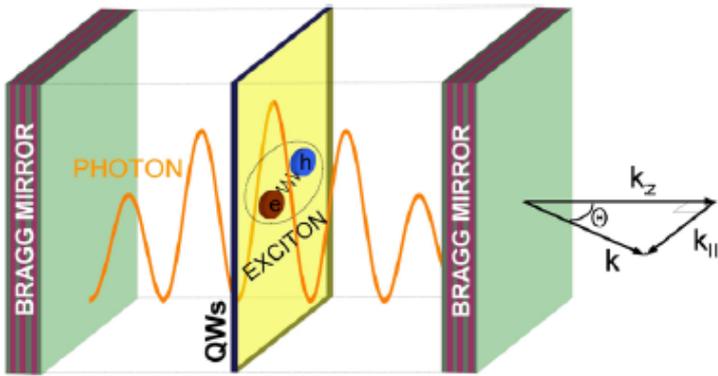
# Semiconductor microcavity structure



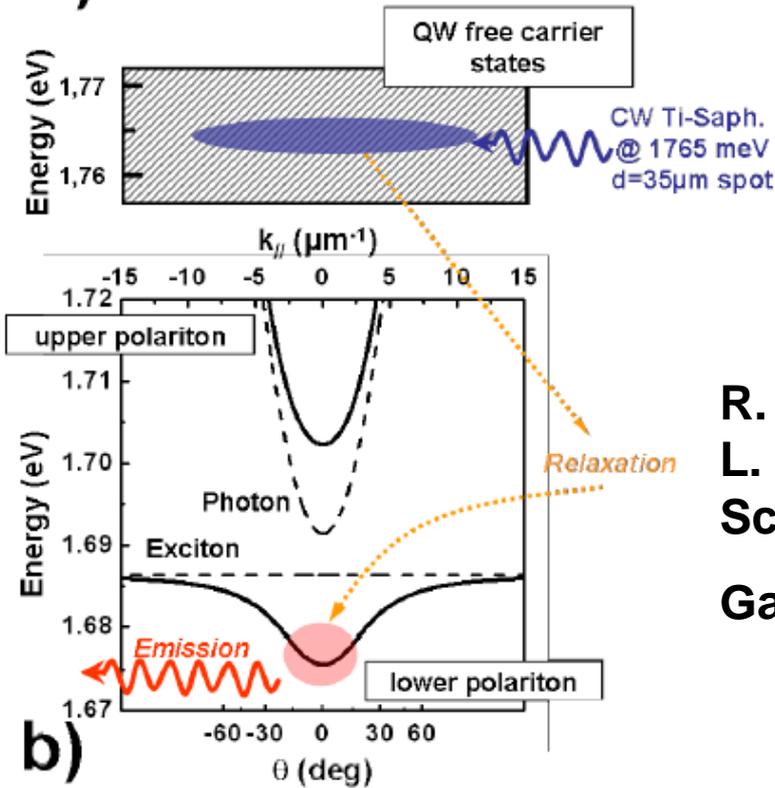
# Polaritons: Matter-Light Composite Bosons

[C. Weisbuch *et al.*, PRL 69 3314 (1992)]





a)



b)

## Microcavity polaritons

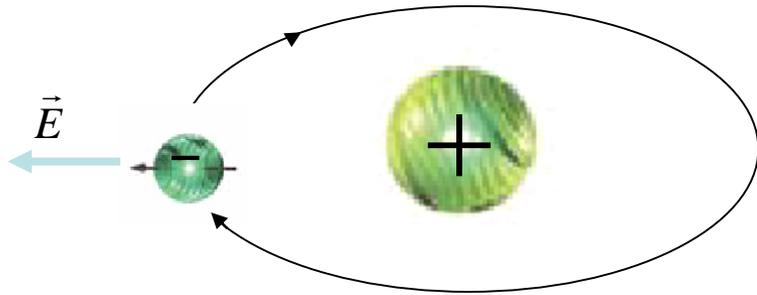
Experiments:  
Kasprzak et al 2006  
CdTe microcavities  
Nature 443, 409 (2006).

R. B. Balili, V. Hartwell, D. W. Snoke,  
L. Pfeiffer and K. West,  
Science 316, 1007 (2007).

GaAs microcavities

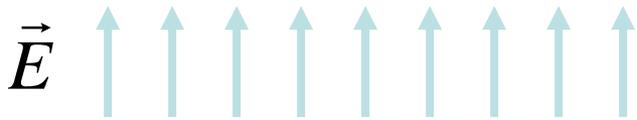
# **The spin Hall effect**

# Relativistic Spin-Orbit Coupling



- Relativistic effect: a particle in an electric field experiences an internal effective magnetic field in its moving frame

$$\vec{B}_{eff} \sim \vec{v} \times \vec{E}$$

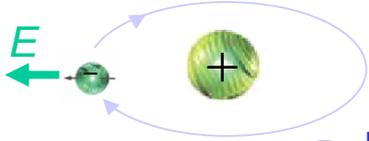


- Spin-Orbit coupling is the coupling of spin with the internal effective magnetic field

$$H \sim -\vec{S} \cdot \vec{B}_{eff}$$

# Spin-orbit coupling (relativistic effect)

Ingredients: - potential  $V(r)$



- motion of an electron

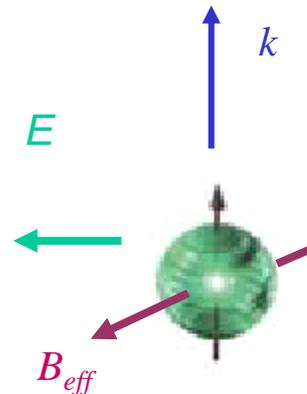
Produces an electric field

$$\vec{E} = -\left(\frac{1}{e}\right)\nabla V(r)$$

In the rest frame of an electron the electric field generates an effective magnetic field

$$\vec{B}_{eff} = -\left(\frac{\hbar\vec{k}}{cm}\right) \times \vec{E}$$

- gives an effective interaction with the electron's magnetic moment



$$H_{SO} = -\vec{\mu} \cdot \vec{B}_{eff}$$

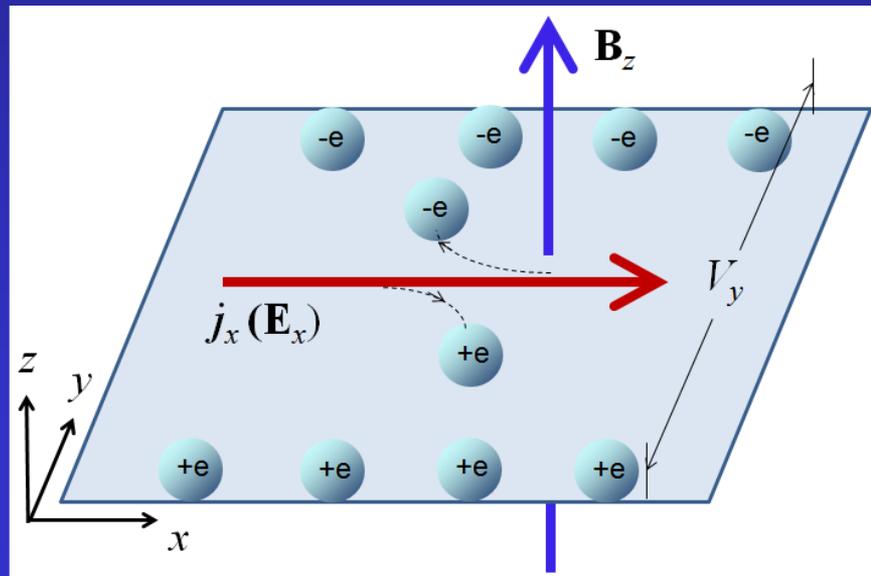
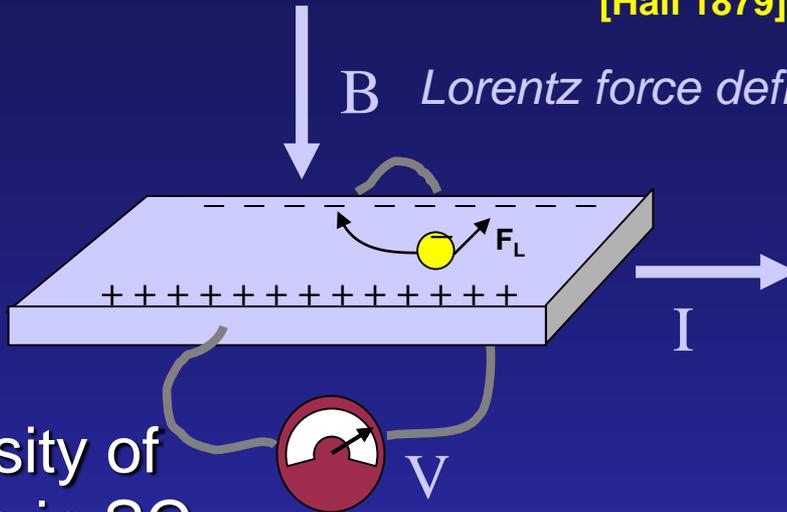
# Ordinary Hall effect

[Hall 1879]

$B$  Lorentz force deflect *like-charge* particles

Ordinary:

Sign and density of carriers; holes in SC

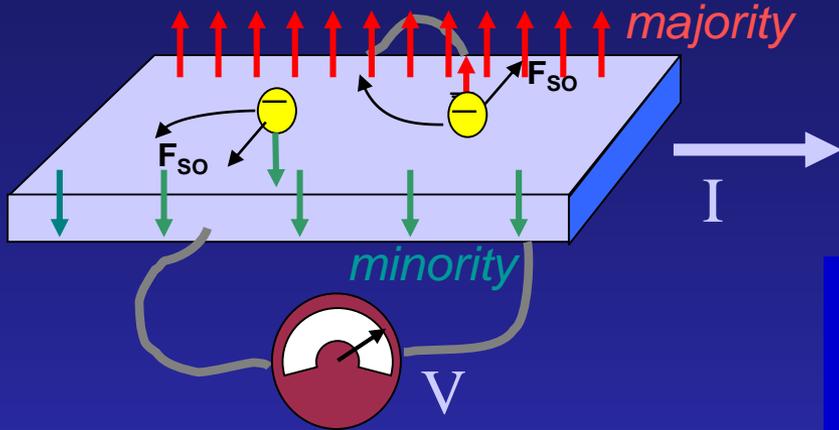


Edwin H. Hall (1855-1938)

# Anomalous Hall effect [Hall, 1880 & 1881]

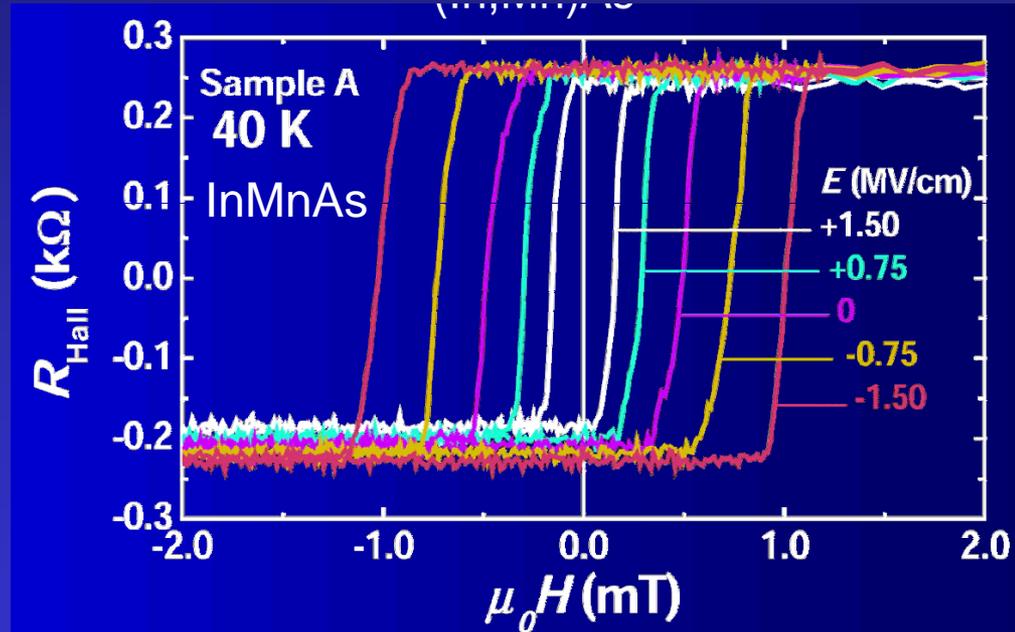
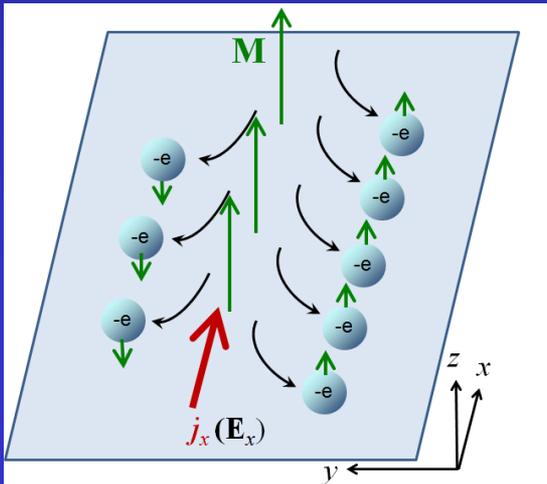
In ferromagnetic materials (and paramagnetic materials in a magnetic field)

Spin-orbit coupling “force” deflects *like-spin* particles



$$\rho_H = R_0 B + 4\pi R_s M$$

Simple electrical measurement of magnetization



D. Chiba *et al.*, Science **301**, 943 (2003)

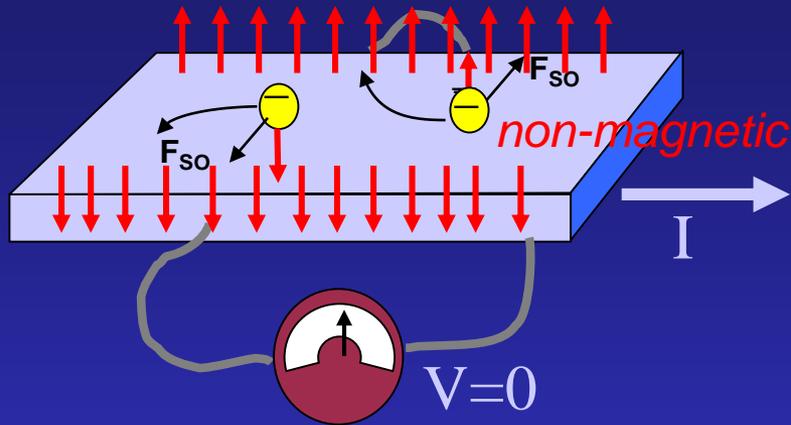
# Spin Hall effect

Dyakonov & Perel, JETP Lett. 13, 467 (1971);  
Zhang, Phys. Rev. Lett. 85, 393 (2000).

Hirsch, Phys. Rev. Lett. 83, 1834 (1999);

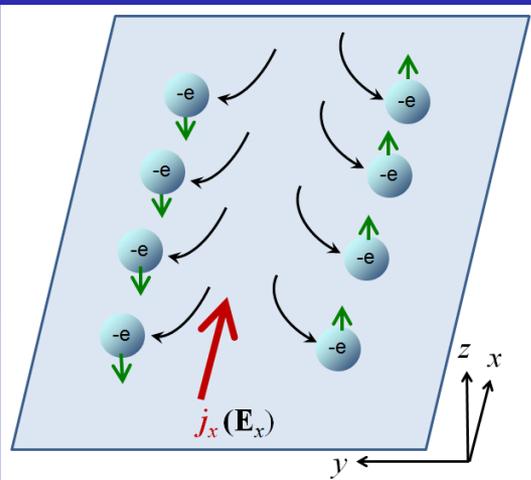
In the systems with strong SOC due either the properties of the electron band structure or scattering on the impurities

*Spin-orbit coupling "force" deflects like-spin particles*



Spin-current generation in non-magnetic systems without applying external magnetic fields

Spin accumulation without charge accumulation excludes simple electrical detection

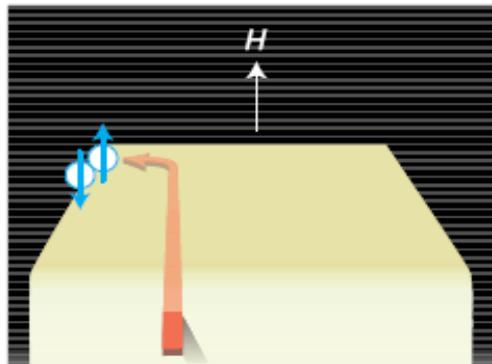


# PERSPECTIVES

PHYSICS

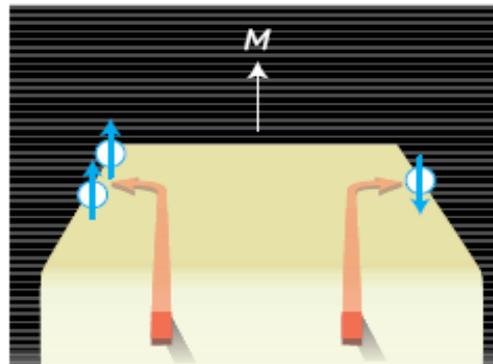
## Taking the Hall Effect for a Spin

Junichiro Inoue and Hideo Ohno



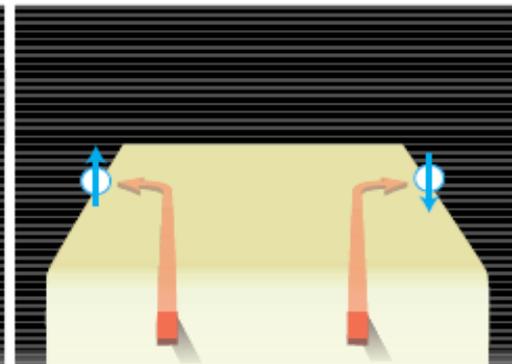
Ordinary Hall effect  
with magnetic field  $H$

Hall voltage but  
no spin accumulation



Anomalous Hall effect  
with magnetization  $M$   
(carrier spin polarization)

Hall voltage and  
spin accumulation



(Pure) spin Hall effect  
no magnetic field necessary

No Hall voltage but  
spin accumulation

# Light-induced effective magnetic fields for ultracold atoms in planar geometries

G. Juzeliūnas, J. Ruseckas, P. Öhberg, and M. Fleischhauer, Physical Review A 73, 025602 (2006)

The effective magnetic field is induced for three-level  $\Lambda$ -type atoms by two counterpropagating laser beams with shifted spatial profiles.

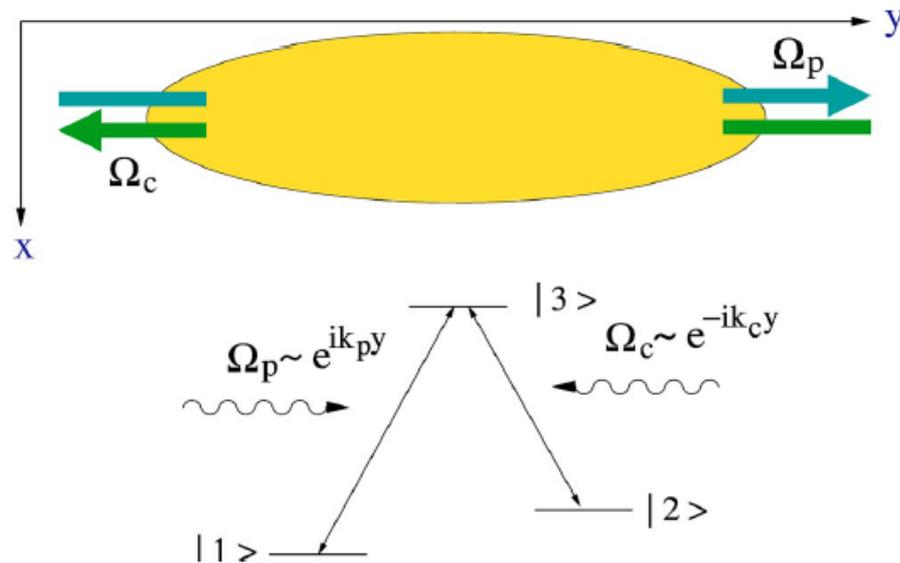


FIG. 1. (Color online) (top) Schematic representation of setup for light-induced effective magnetic fields: Two counterpropagating and overlapping laser beams interact with a cloud of cold atoms. (bottom) The level scheme for the  $\Lambda$ -type atoms interacting with the resonant probe and control beams characterized by Rabi frequencies  $\Omega_p$  and  $\Omega_c$ .

# Transition metal dichalcogenide (TMDC)

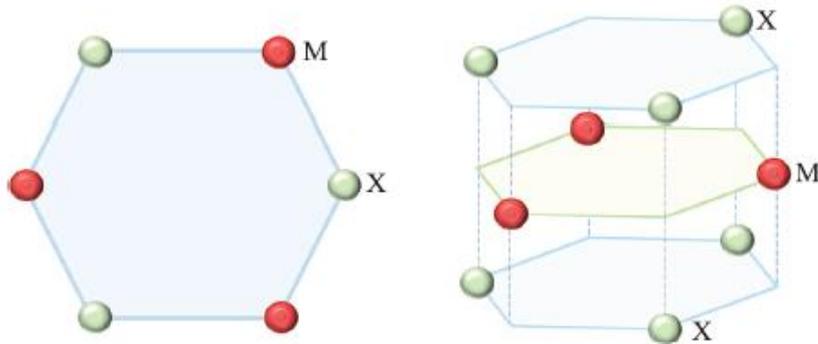
**MoS<sub>2</sub>, MoSe<sub>2</sub>, MoTe<sub>2</sub>, WS<sub>2</sub>, WSe<sub>2</sub>, WTe<sub>2</sub>**

**Review:**

A. Kormanyos, G. Burkard, M. Gmitra, J. Fabian, V. Zolyomi, N. D. Drummond, and V. Fal'ko, 2D Mater. 2, 022001 (2015)

**Excitons in TMDCs:** A. Chernikov, T. C. Berkelbach, H. M. Hill, A. Rigosi, Y. Li, O. B. Aslan, D. R. Reichman, M. S. Hybertsen, and T. F. Heinz, Phys. Rev. Lett. **113**, 076802 (2014).

## The structure of a TMDC monolayer.



## BEC of dipolar excitons in a TMDC double ilayer:

M. M. Fogler, L. V. Butov, and K. S. Novoselov, Nat. Commun. 5, 4555 (2014).

F.-C. Wu, F. Xue, and A. H. MacDonald, Phys. Rev. B 92, 165121 (2015)

## BEC and superfluidity of two-component system of A and B dipolar excitons in a TMDC double layer:

O. L. Berman and R. Ya. Kezerashvili, Phys. Rev. B 93, 245410 (2016). O. L. Berman and R. Ya. Kezerashvili, Physical Review B 96, 094502 (2017).

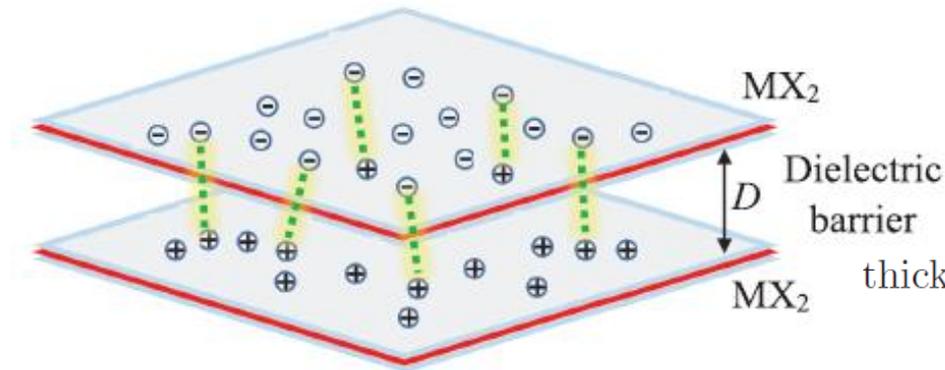
## Spatially separated electrons and holes in a TMDC double layer

**M is a transition metal**

**X is a chalcogenide**

**1. Gap between valence and conduction bands: 1.6 -- 1.8 eV**

**2. No fluctuations of the width of TMDC layers.**



***h*-BN monolayers**

***N<sub>L</sub>* number of monolayers**

$$D = N_L D_{hBN}$$

thickness of one *h*-BN monolayer

$$D_{hBN} = 0.333 \text{ nm}$$

# A and B 2D excitons in a TMDC monolayer

The low-energy effective two-band single-electron Hamiltonian in the form of a spinor with a gapped spectrum for TMDCs in the  $k \cdot p$  approximation:

D. Xiao, G.-B. Liu, W. Feng, X. Xu, and W. Yao, Phys. Rev. Lett. 108, 196802 (2012).

$$\hat{H}_s = at(\tau k_x \hat{\sigma}_x + k_y \hat{\sigma}_y) + \frac{\Delta}{2} \hat{\sigma}_z - \lambda \tau \frac{\hat{\sigma}_z - 1}{2} \hat{s}_z.$$

$$\Delta = 1.6 \text{ -- } 1.8 \text{ eV}$$

$$2\lambda = 0.1 \text{ -- } 0.5 \text{ eV}$$

$\hat{\sigma}$  denotes the Pauli matrices,  $a$  is the lattice constant,  $t$  is the effective hopping integral,  $\Delta$  is the energy gap,  $\tau = \pm 1$  is the valley index,  $2\lambda$  is the spin splitting at the valence band top caused by the spin-orbit coupling (SOC), and  $\hat{s}_z$  is the Pauli matrix for spin

**Strong spin-orbit coupling (SOC) !!!**

T. C. Berkelbach, M. S. Hybertsen, and D. R. Reichman, Phys. Rev. B 88, 045318 (2013):

Significant spin-orbit splitting in the valence band leads to the formation of **A and B excitons in TMDC layers:**

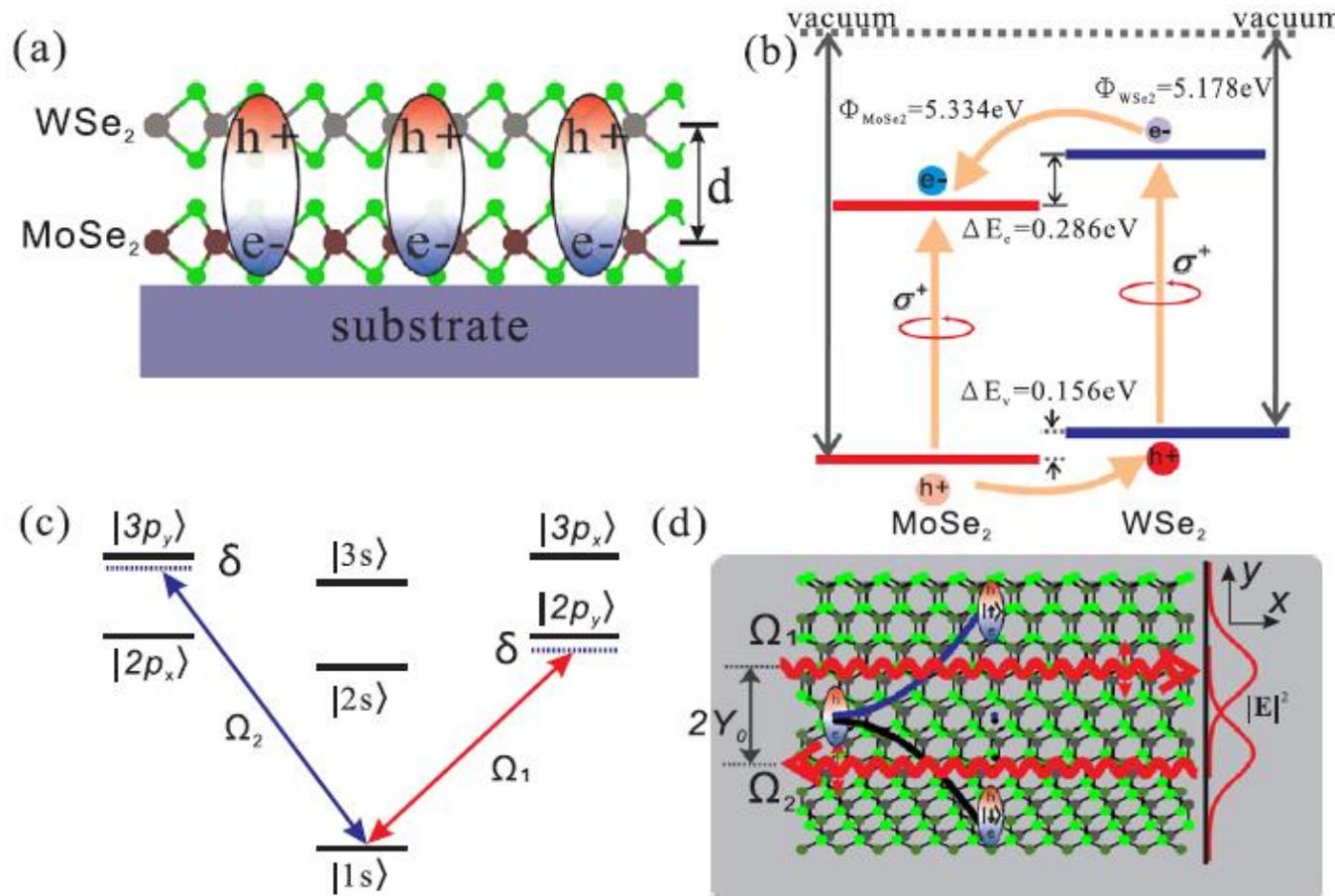
**Type A excitons** are formed by **spin-up electrons from conduction** and **spin-down holes from valence bands**.

**Type B excitons** are formed by **spin-down electrons from conduction** and **spin-up holes from valence bands**.

# Light-Induced Exciton Spin Hall Effect in van der Waals Heterostructure

Y.-M. Li, J. Li, L.-K. Shi, D. Zhang, W. Yang, and K. Chang, Phys. Rev. Lett. 115, 166804 (2015).

A light-induced spin Hall effect for interlayer exciton gas in monolayer MoSe<sub>2</sub>-WSe<sub>2</sub> van der Waals heterostructure. By applying two infrared, spatially varying laser beams coupled to the exciton internal states, a spin-dependent gauge potential on the exciton center-of-mass motion is induced. This gauge potential deflects excitons in different spin states towards opposite directions, leading to a finite spin current.



# Trapping Cavity Polaritons

# Cavity polaritons in TMDC:

## Experiments:

D. W. Snoke, Science 298, 1368 (2002).

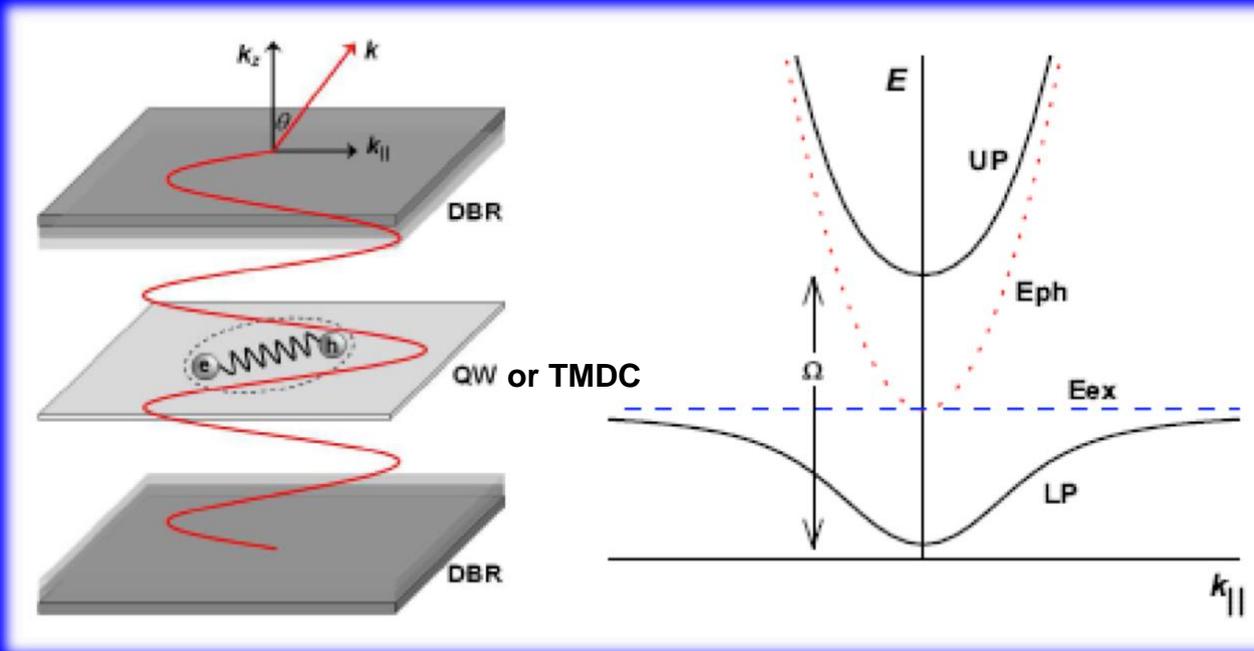
P. Littlewood, Science 316, 989 (2007).

D. W. Snoke and J. Keeling, Phys. Today 70, 54 (2017).

X. Liu, et al., Nat. Photonics 9, 30 (2015).

L. C. Flatten, et al., Sci. Rep. 6, 33134 (2016).

S. Dufferwiel, et al., Nature Commun. 6, 8579 (2015).



cavity photon:

$$E = \hbar c \sqrt{k_z^2 + k_{||}^2} = \hbar c \sqrt{(\pi / L)^2 + k_{||}^2}$$

quantum well exciton:

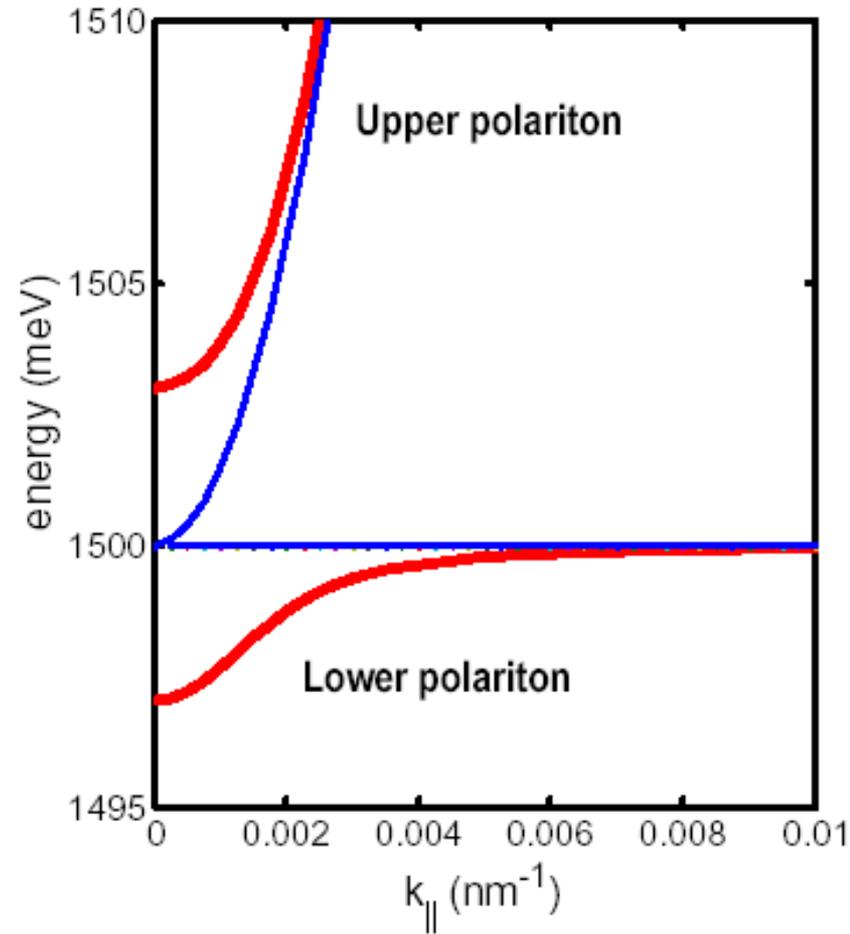
$$E = E_{gap} - \Delta_{bind} + \frac{\hbar^2 N^2}{2m_r (2L)^2} + \frac{\hbar^2 k_{||}^2}{2m}$$

# Elementary model of polariton modes

**exciton** → **polariton**  
**photon** → **polariton**

$$H_k = \begin{pmatrix} E_k^{(cav)} & \hbar\Omega_R \\ \hbar\Omega_R^* & E_k^{(exc)} \end{pmatrix}$$

$$E_k^{(\pm)} = \frac{E_k^{(cav)} + E_k^{(exc)}}{2} \pm \frac{1}{2} \sqrt{\left(E_k^{(cav)} - E_k^{(exc)}\right)^2 + 4|\hbar\Omega_R|^2}$$



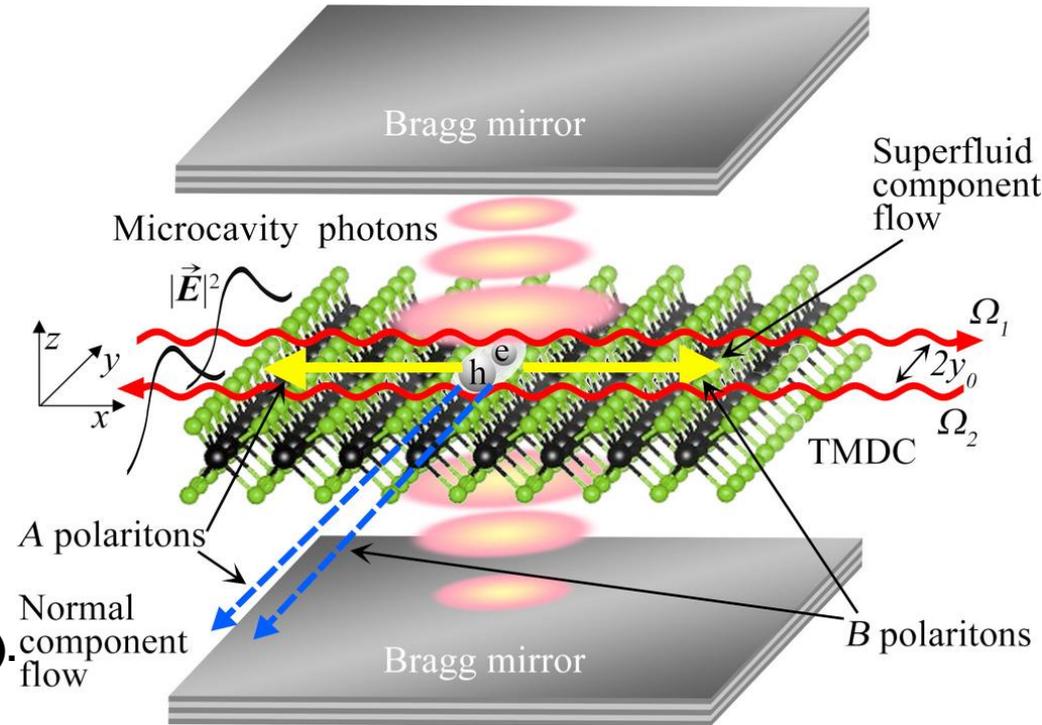
Realistic model includes finite polariton lifetime, leaky modes in the mirrors, etc.

P. B. Littlewood, P. R. Eastham, J. M. J. Keeling, F. M. Marchetti, B. D. Simons, and M. H. Szymanska, *J. Phys.: Condens. Matter* **16**, S3597–S3620 (2004) .

# We predict the Spin Hall effect (SHE) for microcavity polaritons in TMDC

O. L. Berman, R. Ya. Kezerashvili, and Yu. E. Lozovik, Physical Review B 99, 085438 (2019).

1. The polaritons cloud is formed due to the coupling of excitons created in a TMDC layer and microcavity photons.
2. Two coordinate-dependent, counterpropagating and overlapping laser beams in the plane of the TMDC layer interact with a cloud of polaritons.
3. The counterpropagating and overlapping laser beams, characterized by Rabi frequencies  $\Omega_1$  and  $\Omega_2$  produce the spin-dependent gauge magnetic and electric fields due to strong SOC for electron and holes in TMDC.



Y.-M. Li, et al., Phys. Rev. Lett. 115, 166804 (2015).

4. The gauge magnetic field deflects the exciton component of polaritons consisting from the excitons with different spin states of charge carriers, namely **A** and **B** excitons, towards opposite directions.
5. For the laser pumping frequencies, corresponding to the resonant excitations of one type of excitons (**A** or **B**), the corresponding excitons together with coupled to them photons form polaritons, which deflect to opposite transverse directions.

Using circular polarized pumping, one can excite both **A** and **B** excitons in one valley simultaneously.

G. Wang, et al., Rev. Mod. Phys. 90, 021001 (2018).

6. The normal components of the **A** and **B** polariton flows slightly deflect in opposite directions and propagate almost perpendicularly to the counterpropagating beams.

7. In contrast, the superfluid components of the **A** and **B** polariton flows propagate in opposite directions along the counterpropagating beams.

# Hamiltonian of microcavity polaritons in gauge fields

O. L. Berman, R. Ya. Kezerashvili, and Yu. E. Lozovik, Physical Review B 99, 085438 (2019).

The Hamiltonian of TMDC polaritons in the presence of counterpropagating and overlapping laser beams:

$$\hat{\mathcal{H}} = \hat{H}_{\text{exc}} + \hat{H}_{\text{ph}} + \hat{H}_{\text{exc-ph}} + \hat{H}_{\text{exc-exc}}$$

The Hamiltonian of TMDC excitons:  $\hat{H}_{\text{exc}} = \sum_{\mathbf{P}} \varepsilon_{\text{ex}}(\mathbf{P}) \hat{b}_{\mathbf{P}}^{\dagger} \hat{b}_{\mathbf{P}}$

$$\varepsilon_{\text{ex}}(\mathbf{P}) = E_{\text{bg}} - E_b + \varepsilon_0(\mathbf{P})$$

$E_{\text{bg}}$  is the band gap energy

$$\varepsilon_0(\mathbf{P}) = \frac{(\mathbf{P} - \mathbf{A}_{\sigma})^2}{2M}$$

$E_b$  is the binding energy of an exciton

Hamiltonian of microcavity photons:

$$\hat{H}_{\text{ph}} = \sum_{\mathbf{P}} \varepsilon_{\text{ph}}(P) \hat{a}_{\mathbf{P}}^{\dagger} \hat{a}_{\mathbf{P}}$$

$$\varepsilon_{\text{ph}}(P) = (c/\tilde{n}) \sqrt{P^2 + \hbar^2 \pi^2 q^2 L_C^{-2}}$$

$L_C$  is the length of the cavity,  $\tilde{n} = \sqrt{\epsilon}$  is index of refraction of the microcavity,  $q$  is the longitudinal mode number.

Effective mass of microcavity photons:

$$m_{\text{ph}} = \hbar \pi q / ((c/\tilde{n}) L_C)$$

Hamiltonian of exciton-photon coupling:

$$\hat{H}_{\text{exc-ph}} = \hbar \Omega_R \sum_{\mathbf{P}} \hat{a}_{\mathbf{P}}^{\dagger} \hat{b}_{\mathbf{P}} + \text{H.c.}$$

$\Omega_R$  is the Rabi splitting constant

where  $M$  is the mass of an exciton and  $\mathbf{A}_{\sigma}$  is the gauge vector potential acting on the exciton component of polaritons, associated with different spin states of the conduction band electron, forming an exciton,  $\sigma = \uparrow$  and  $\downarrow$ .

After applying the unitary transformations of the Hamiltonian at  $H_{\text{exc-exc}} = 0 \rightarrow$

The Hamiltonian of lower polaritons:

$$\hat{\mathcal{H}}_0 = \sum_{\mathbf{P}} \varepsilon_{LP}(\mathbf{P}) \hat{P}_{\mathbf{P}}^{\dagger} \hat{P}_{\mathbf{P}}$$

effective vector and scalar potentials, respectively, acting on polaritons,  $\mathbf{A}_{\sigma}^{(eff)}$  and  $V^{(eff)}$

$$\varepsilon_{LP}(\mathbf{P}) = \hbar \pi q L_C^{-1} - |\hbar \Omega_R| + \varepsilon(\mathbf{P})$$

$$\alpha \equiv 1/2(M^{-1} + (c/\tilde{n})L_C/\hbar \pi q)P^2/|\hbar \Omega_R| \ll 1$$

$$\varepsilon(\mathbf{P}) = \frac{(\mathbf{P} - \mathbf{A}_{\sigma}^{(eff)})^2}{2M_p} + V^{(eff)}$$

$$\mathbf{A}_{\sigma}^{(eff)} = \frac{m_{\text{ph}} \mathbf{A}_{\sigma}}{M + m_{\text{ph}}}, \quad V^{(eff)} = \frac{A_{\sigma}^2}{4(M + m_{\text{ph}})}$$

$$M_p = 2\mu, \quad \mu = M m_{\text{ph}} / (M + m_{\text{ph}})$$

# The dependence of the effective gauge magnetic $B^{(eff)}$ and electric $E^{(eff)}$ fields on the parameter $l$ .

$$\mathbf{B}_\sigma^{(eff)} = \nabla_{\mathbf{R}} \times \mathbf{A}_\sigma^{(eff)} = \frac{-\eta_\sigma \hbar m_{ph} (|k_1| + |k_2|)}{4l(M + m_{ph})} \mathbf{e}_z, \quad \mathbf{E}^{(eff)} = -\nabla_{\mathbf{R}} V^{(eff)} = -\frac{\hbar^2 (|k_1| + |k_2|)^2}{16l(M + m_{ph})} \mathbf{e}_y.$$

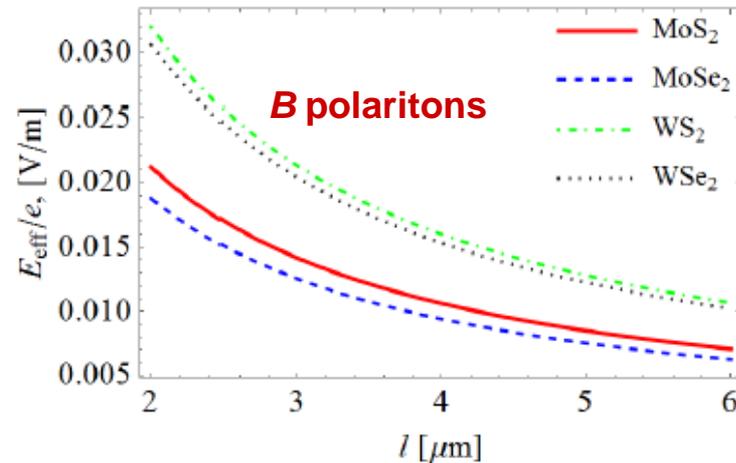
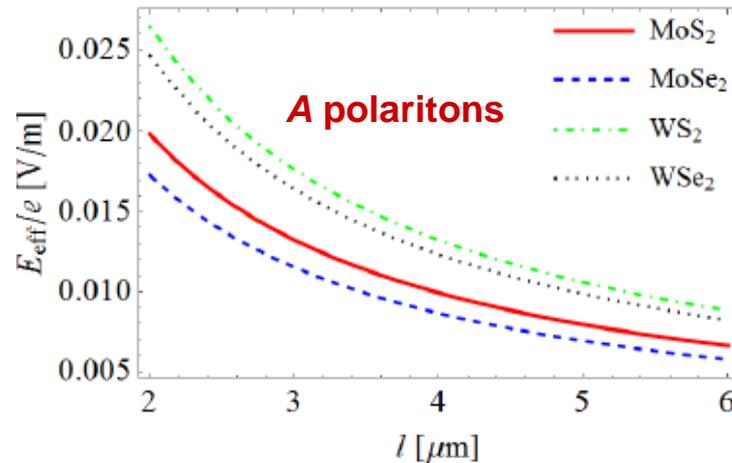
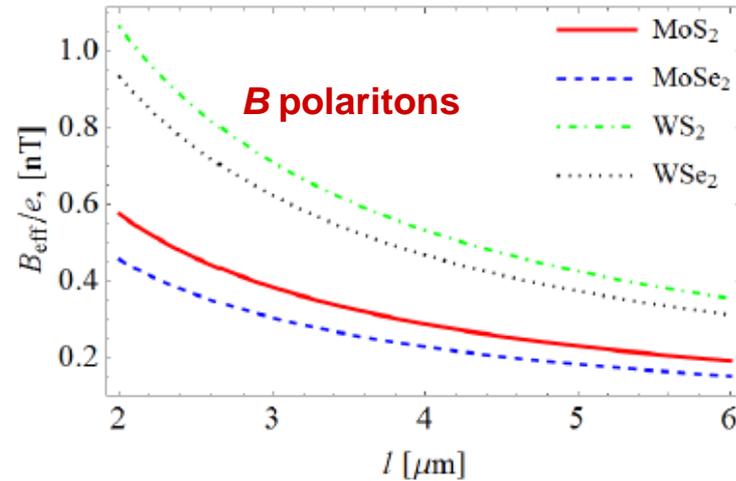
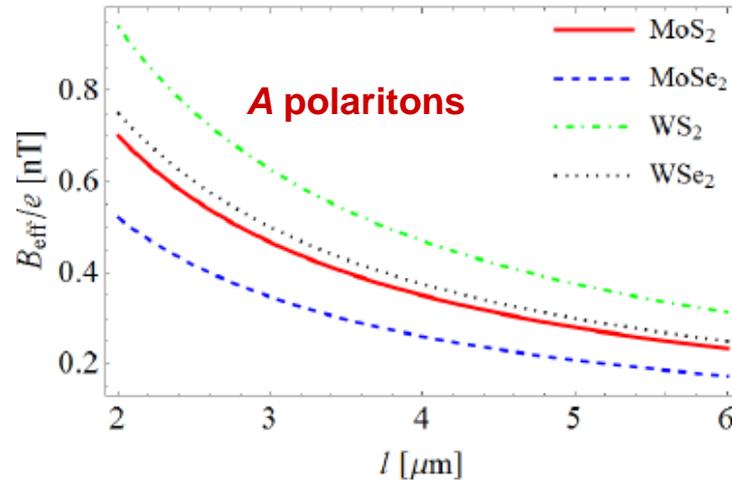
$\eta_\uparrow = 1$  for an  $A$  exciton and  $\eta_\downarrow = -1$  for a  $B$  exciton.

Calculations performed for  $|k_1| + |k_2| = 3 \mu\text{m}^{-1}$

$M$  is an exciton mass;  $m_{ph}$  is a microcavity photon mass

$l = a^2/8y_0$ ,  $a = 10 \mu\text{m}$  is the beam width,

$y_0$  is the spatial shift of two laser beams



# Conductivity tensor for non-interacting polaritons

**Drude model:**

$$\frac{d\mathbf{P}}{dt} = \mathbf{E}^{(\text{eff})} + \mathbf{v} \times \mathbf{B}_\sigma^{(\text{eff})} - \frac{\mathbf{P}}{\tau}$$

For a steady state, setting  $d\mathbf{P}/dt = 0$ ,

$$\mathbf{P} = M_p \mathbf{v}$$

$\mathbf{v}$  is the velocity and  $\tau$  is a scattering time of microcavity polaritons.

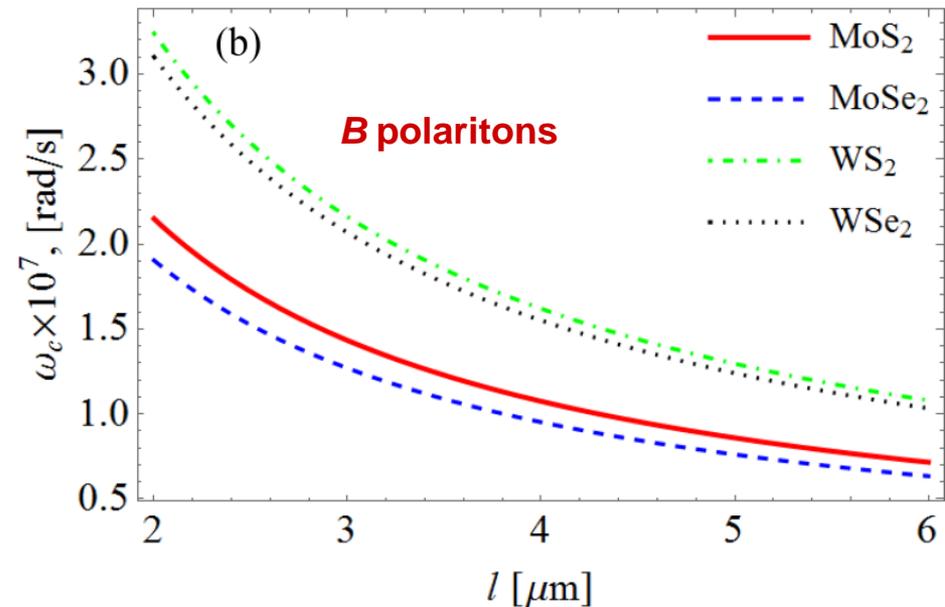
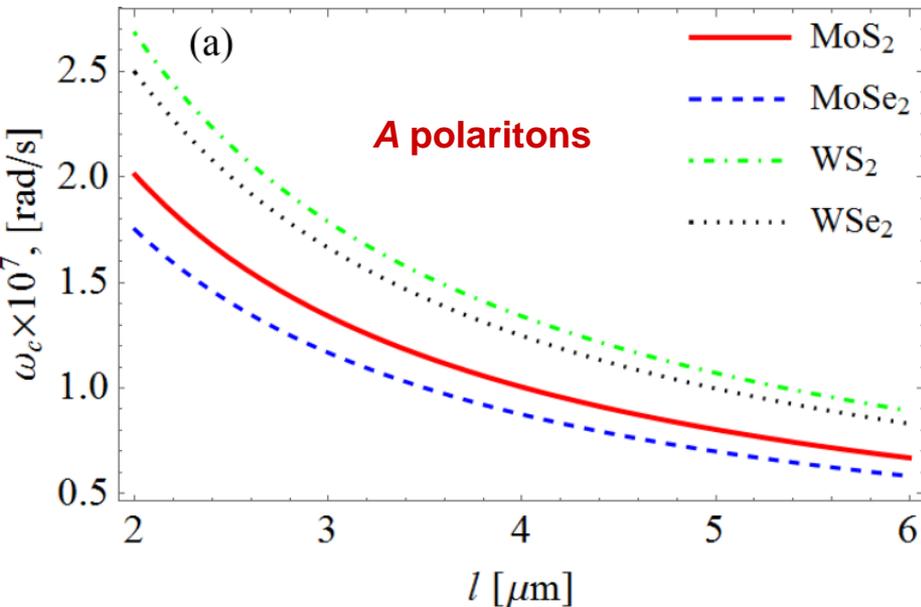
linear polariton flow density is defined as  $\mathbf{j} = n\mathbf{v}$       $\mathbf{E}^{(\text{eff})} = \frac{M_p}{n\tau} \mathbf{j} - \frac{\mathbf{j} \times \mathbf{B}_\sigma^{(\text{eff})}}{n}$

$2 \times 2$  resistivity matrix  $\rho_\sigma$  can be defined as  $\mathbf{E}^{(\text{eff})} = \rho_\sigma \mathbf{j}$ ,

The conductivity tensor  $\tilde{\sigma}_\sigma$  is defined as the inverse matrix to the resistivity matrix  $\rho_\sigma$ .

$$\sigma_{\sigma xx} = \sigma_{\sigma yy} = \frac{\sigma_0}{1 + \omega_c^2 \tau^2}, \quad \sigma_{\sigma xy} = -\sigma_{\sigma yx} = -\frac{\eta_\sigma \sigma_0 \omega_c \tau}{1 + \omega_c^2 \tau^2},$$

$\sigma_0 = \tau n / M_p$  and  $\omega_c = B^{(\text{eff})} / M_p$  is the cyclotron frequency.



$l = a^2 / 8y_0$ ,  $a = 10 \mu\text{m}$  is the beam width,

Calculations performed for  $|k_1| + |k_2| = 3 \mu\text{m}^{-1}$

# Conductivity tensor for superfluid polaritons

Weakly interacting Bose gas of polaritons in dilute regime below  $T_c$  is **superfluid**

$n_n$  is the concentration of **the normal component**

$$n_s(T) = n - n_n(T)$$

$n_s$  is the concentration of **the superfluid component**

$$n_n(T) = \frac{3\zeta(3) k_B^3 T^3}{2\pi \hbar^2 c_s^4 M_p}$$

$n$  is the **total concentration**

The polaritons in the superfluid component do not collide.  $\tau \rightarrow +\infty$ .

**Drude model:**  $M_p \frac{dv_x}{dt} = -\eta_\sigma B^{(eff)} v_y, \quad M_p \frac{dv_y}{dt} = E^{(eff)} + \eta_\sigma B^{(eff)} v_x$

steady state, which corresponds to  $dv_x/dt = dv_y/dt = 0$   $v_y = 0$

the linear superfluid polariton flow density  $\mathbf{j}^{(s)} = n_s \mathbf{v}$ .  $v_x = -E^{(eff)} / \eta_\sigma B^{(eff)}$

conductivity tensor  $\tilde{\sigma}_\sigma^{(s)}(T)$  for the superfluid

$$\sigma_{\sigma xx}^{(s)} = \sigma_{\sigma yy}^{(s)} = 0, \quad \sigma_{\sigma xy}^{(s)}(T) = -\sigma_{\sigma yx}^{(s)}(T) = -\frac{n_s(T)}{\eta_\sigma B^{(eff)}}$$

For the conductivity tensor  $\tilde{\sigma}_\sigma^{(n)}(T)$  for the normal component

$$\sigma_0(T) = \tau n_n(T) / M_p$$

**The sound spectrum of collective excitations:**  $\epsilon(P) = c_s P$

**with the sound velocity  $c_s$**

O. L. Berman, R. Ya. Kezerashvili, and Yu. E. Lozovik,  
Phys. Rev. B, 99, 085438 (2019).

# Linear polariton flow density

1. Our calculations show that the contribution to the Hall linear polariton flow density from the superfluid component essentially exceeds the one from the normal component.
2. The contribution to the Hall linear polariton flow density from the superfluid component does not depend on the distance  $l$  between the counterpropagating laser beams.
3. The contribution to the linear polariton flow density from the superfluid component in the direction of the effective gauge electric field ( $y$  direction) is zero.

At the temperature  $T = 300$  K for A polaritons we have obtained the total Hall linear polariton flow density in the presence of superfluidity  $j_x^{(tot)} = 8.51887 \times 10^{13} \text{ nm}^{-1}\text{s}^{-1}$  for MoS<sub>2</sub>;  $j_x^{(tot)} = 9.54342 \times 10^{13} \text{ nm}^{-1}\text{s}^{-1}$  for MoSe<sub>2</sub>,  $j_x^{(tot)} = 9.76334 \times 10^{13} \text{ nm}^{-1}\text{s}^{-1}$  for WS<sub>2</sub>,  $j_x^{(tot)} = 1.1415 \times 10^{14} \text{ nm}^{-1}\text{s}^{-1}$  for WSe<sub>2</sub>.

## Proposed experiment

O. L. Berman, R. Ya. Kezerashvili, and Yu. E. Lozovik, Physical Review B 99, 085438 (2019).

1. The proposed experiment for observation of the spin Hall effect for microcavity polaritons is related to the measurement of the angular distribution of the photons escaping the optical microcavity.
2. In the absence of the effective gauge magnetic and electric fields, the angular distribution of the photons escaping the microcavity is central-symmetric with respect to the perpendicular to the Bragg mirrors.
3. We obtain the average tangent of the angles  $\alpha$  of deflection for the polariton flow in the  $(x, y)$  plane of the microcavity:

$$\overline{\tan \alpha} = \left| \frac{j_x}{j_y} \right| = \left| \frac{\sigma_{\sigma xy}}{\sigma_{\sigma yy}} \right|$$

Without superfluidity:

$$\overline{\tan \alpha} = \omega_c \tau$$

# Proposed experiment for observation of the SHE for microcavity polaritons in the presence of superfluidity

For the normal component:

$$\overline{\tan \alpha^{(n)}} = \left| \frac{j_x^{(n)}}{j_y^{(n)}} \right| = \left| \frac{\sigma_{\sigma xy}^{(n)}}{\sigma_{\sigma yy}^{(n)}} \right| = \omega_c \tau$$

Calculations performed for  $|k_1| + |k_2| = 3 \mu\text{m}^{-1}$

$l = a^2 / 8y_0$ ,  $a = 10 \mu\text{m}$  is the beam width,

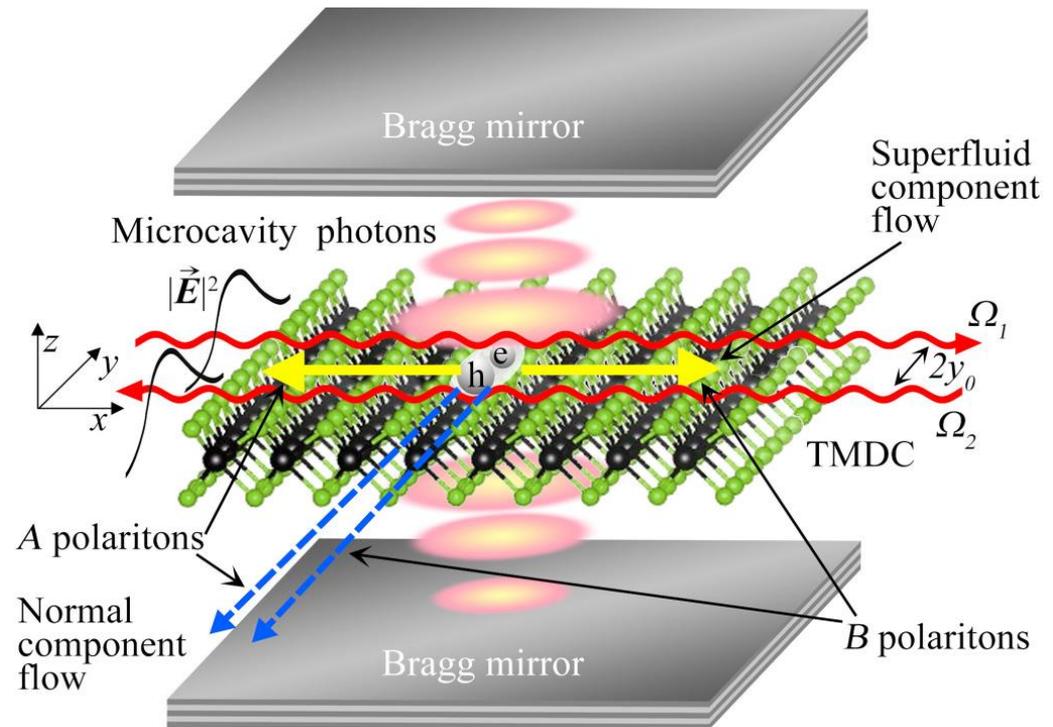
$$\overline{\tan \alpha^{(n)}} \approx 10^{-5}, \text{ and } \overline{\alpha^{(n)}} \approx 10^{-3} \text{ } ^\circ$$

For the superfluid component:

$$\overline{\tan \alpha^{(s)}} = \left| \frac{j_x^{(s)}}{j_y^{(s)}} \right| = \left| \frac{\sigma_{\sigma xy}^{(s)}}{\sigma_{\sigma yy}^{(s)}} \right| \rightarrow +\infty$$

$$\sigma_{\sigma yy}^{(s)} = 0$$

$$\overline{\alpha^{(s)}} = 90^\circ$$



O. L. Berman, R. Ya. Kezerashvili, and Yu. E. Lozovik, Phys. Rev. B, 99, 085438 (2019).

**SHE for microcavity polaritons allows to separate the superfluid component from the normal components of the polariton flow!**

# Conclusions

O. L. Berman, R. Ya. Kezerashvili, and Yu. E. Lozovik, Physical Review B, 99, 085438 (2019).

- We have predicted **the spin Hall effect for microcavity polaritons**, formed by excitons **in a TMDC** and microcavity photons.
- We demonstrated that **the polariton flow** can be achieved by generation **the effective gauge vector and scalar potentials**, acting on polaritons.
- We have obtained the components of polariton conductivity tensor for both non-interacting polaritons **without BEC** and for weakly-interacting Bose gas of polaritons **in the presence of BEC and superfluidity**.
- We demonstrated that due to the **SHE** the polariton flows in the same valley are splitting: **the normal components** of the *A* and *B* polariton flows **slightly deflect** in opposite directions and propagate **almost perpendicularly to the counterpropagating beams**, while the **superfluid components** of the *A* and *B* polariton flows propagate in opposite directions **along the counterpropagating beams**.
- We predicted **the method to separate the superfluid component** from the **normal component** of the polariton flow due to the **SHE**.

## I wish to thank my co-authors



Prof. Roman Ya. Kezerashvili  
City Tech, City University of New York



Prof. Yurii E. Lozovik  
Institute of Spectroscopy

The work was supported by US Department of Defense under  
Grant No. W911NF1810433  
and PSC CUNY  
under Grant No. 60599-00 48.

